

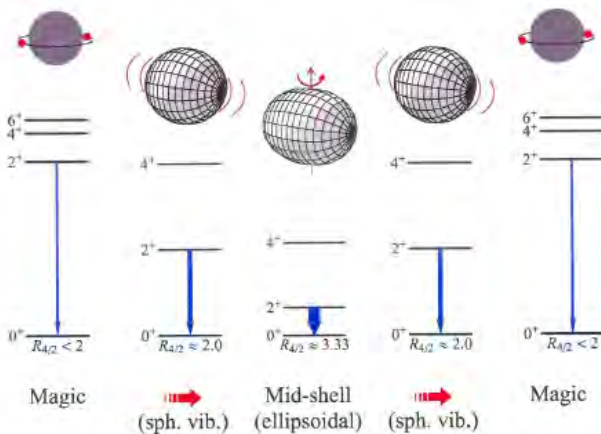
Chasing $B(E2)_{4_1^+/2_1^+}$ Anomaly

Bahadır Saygı

Ege University

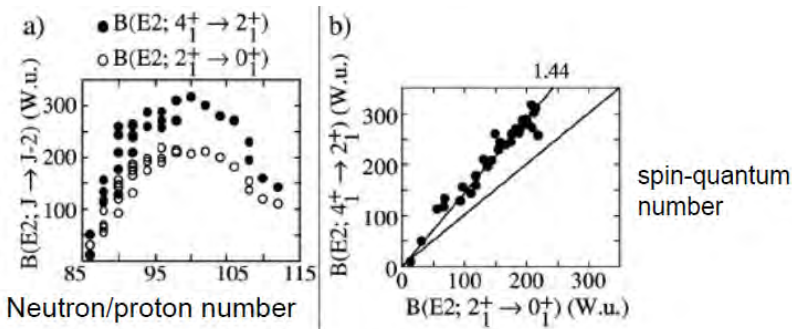
04/06/2021

- How the structure evolve as a function of
 - Spin-Quantum number ?
 - Proton/Neutron number or $N_p N_n$ Number ?



Which parameter we look in detail to deduce the structure of a nucleus of interest ?

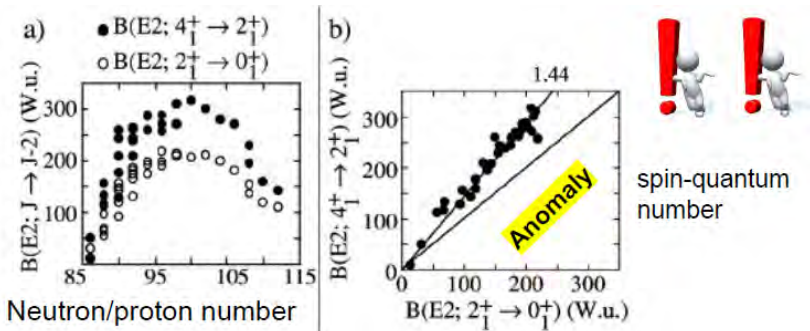
- We measure $B(E2)$ values - Reduced transition probability
 - A direct measure of deformation
 - Behavior of $B(E2)$ values a function of spin-quantum or neutron/proton numbers play a key role to understand the nuclei of interest.



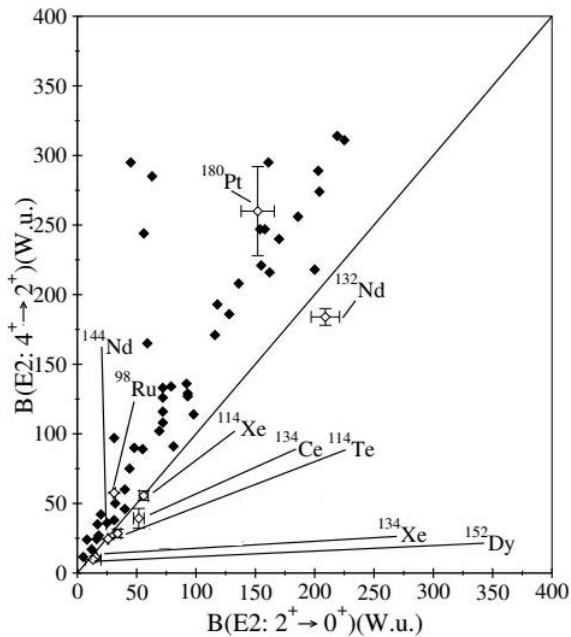
Cakirli, R. et al. Phys. Rev. C, 70, 047302

Which parameter we look in detail to deduce the structure of a nucleus of interest ?

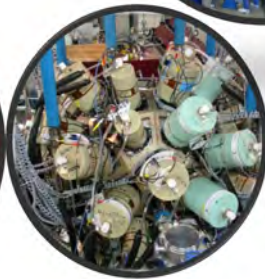
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Cakirli, R. et al. Phys. Rev. C, 70, 047302



Set-Up

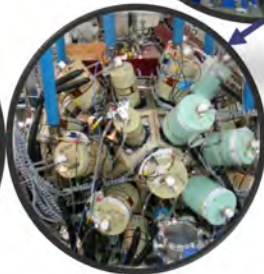




GREAT
Focal plane
spectrometer



RITU
Gas-filled recoil separator



JUROGAM II Array





GREAT
Focal plane
spectrometer



RITU
Gas-filled recoil separator



JUROGAM II Array





GREAT
Focal plane
spectrometer

RITU

Gas-filled recoil separator,
transmission 20-50%



RITU
Gas-filled recoil separator

TDR

Total Data Readout, triggerless data
acquisition system with 10 ns time
stamping



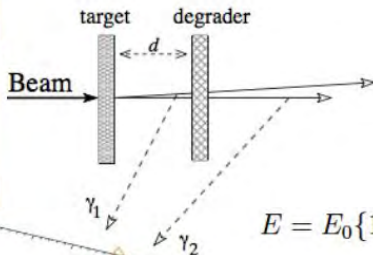
K130 Cyclotron
BEAM DIRECTION



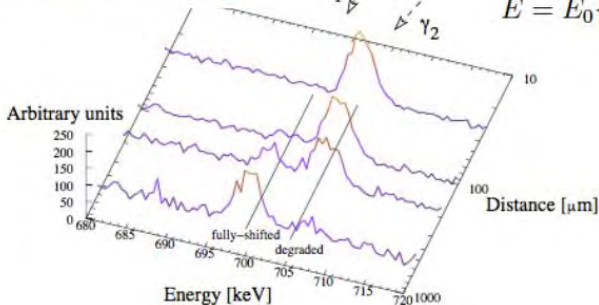
JUROGAM II
24+15 Ge+BGO
detectors, eff. 6%

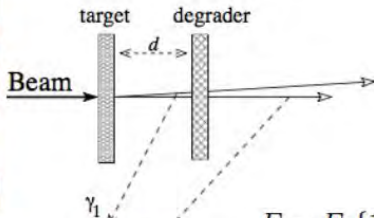
JUROGAM II Array

Recoil Distance Doppler Shift Technique

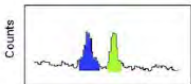
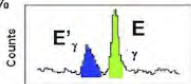
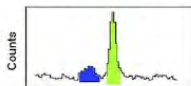
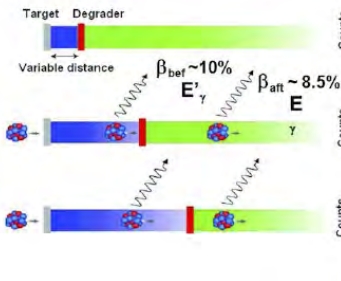


$$E = E_0 \left\{ 1 + \frac{v}{c} \cos \theta \right\}$$

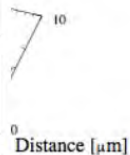




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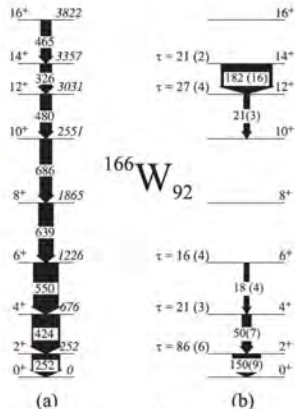
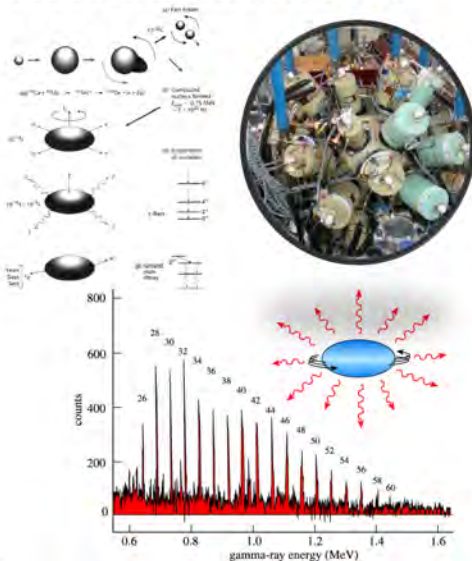


Energy



Reaction Mechanism

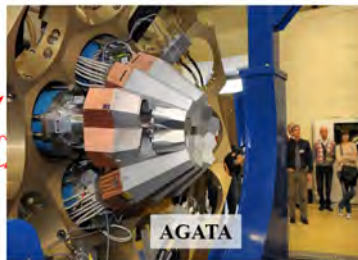
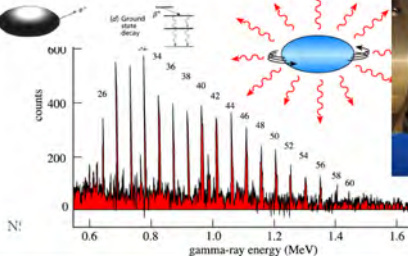
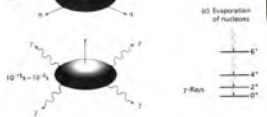
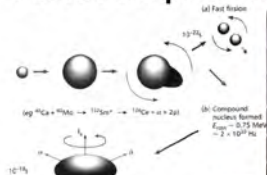
Fusion Evaporation Reaction



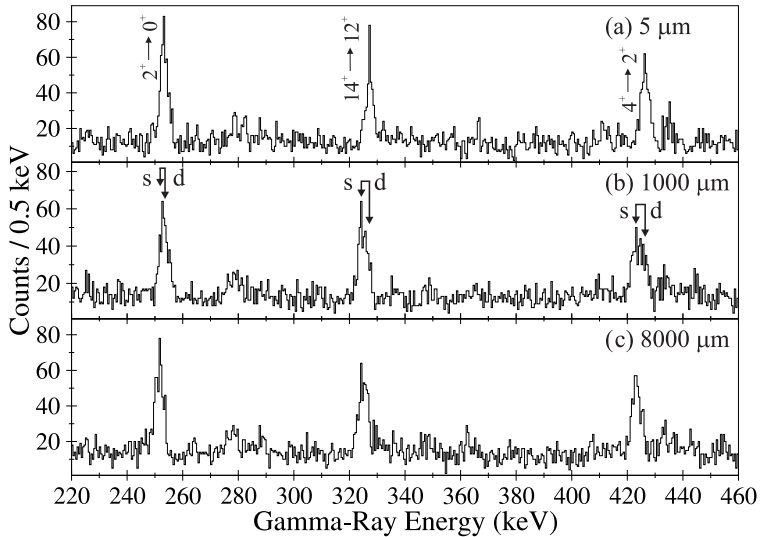
$$B(E2) = \frac{0.0816}{E_{\gamma}^5 (1 + a_{\text{tot}})^2} \tau^{-2} \ln^2$$

Reaction Mechanism

Fusion Evaporation Reaction



- Excited states in ^{166}W were populated using the $^{92}\text{Mo}(^{78}\text{Kr},4\text{p})$ reaction.
- A 380 MeV $^{78}\text{Kr}^{15+}$ beam provided by the K130 cyclotron at the University of Jyväskylä Accelerator Laboratory bombarded a 0.6 mg/cm^2 ^{92}Mo target.
- A nominal beam intensity of 3 pA was delivered to the target.



Differential Decay Curve Method

$$\tau = \frac{Q_{\text{depop}}^d(x) - Q_{\text{feed}}^d(x)}{v \frac{d}{dx} [Q_{\text{depop}}^s(x)]},$$

where $Q_j^i(x) = I_j^i / (I_j^s + I_j^d)$ and $I_j^i(x)$ are the γ -ray intensities for the shifted ($i = s$) and degraded ($i = d$) components measured at the target-to-degrader distance x for the depopulating ($j = \text{depop}$) and feeding ($j = \text{feed}$) transitions, respectively.

A. Dewald et al. Prog in Part and Nucl Phys 67, 3, 2012, 786

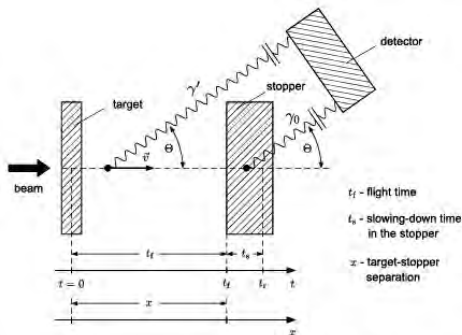
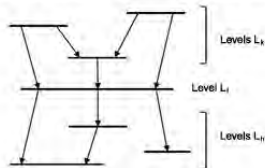
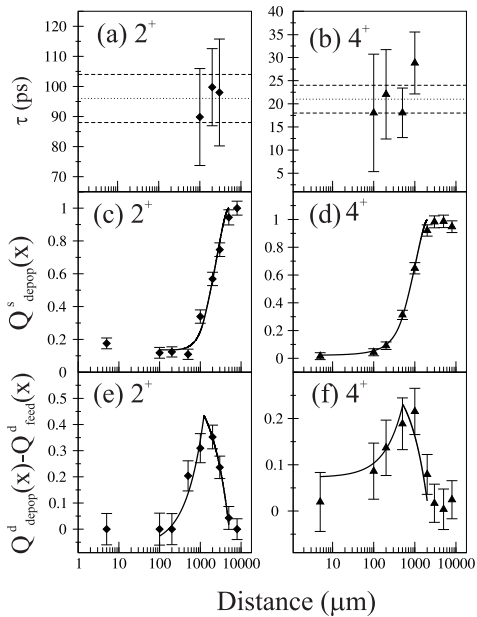


Fig. 1. Schematic description of the Recoil Distance Doppler-Shift method.



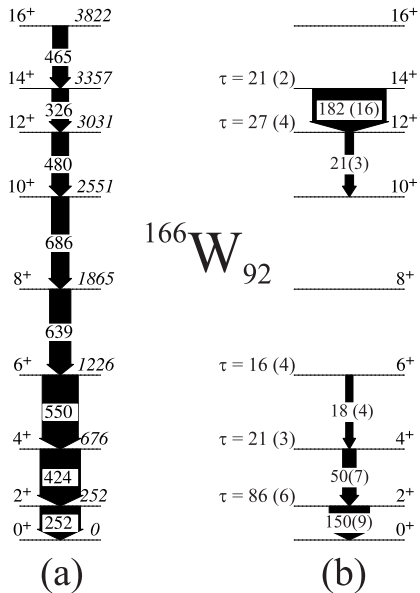


$$T(E\lambda; i \rightarrow f) = \frac{1}{\tau} = \frac{8\pi}{\hbar} \frac{\lambda + 1}{\lambda[(2\lambda + 1)!!]^2} k^{2\lambda+1} B(\lambda; i \rightarrow f),$$

$$B(E\lambda; i \rightarrow f) = \frac{F_{\lambda}^{(E)}}{(E_{\gamma})^{2\lambda+1} \tau} e^2 \cdot b^{\lambda}$$

$$B(E2) = \frac{0.0816}{(E_{\gamma})^5 \tau (1 + \alpha_{\gamma})} e^2 b^2.$$

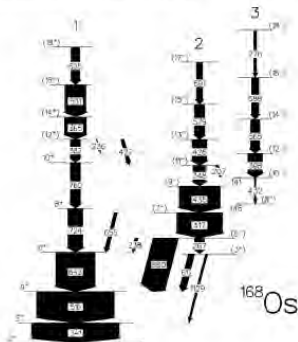
$$1W.u. = (5.94 \times 10^{-6}) A^{4/3} e^2 b^2 .$$



B. Saygı et al Phys. Rev. C, 96, 021301 (R).

$B(E2)_{4_1^+/2_1^+} \approx f(P.N)$ ^{168}Os Case

- $^{78}\text{Kr}^{15+} + ^{92}\text{Mo}$ @345 using K130 2p exit channel
- Employed RDDS in junction with plunger in the target chamber
- Measured τ values of 2^+ and 4^+



6^+ 1833

6^+ 1499.1

4^+ 857.3

$B(E2) = 27(9)$

2^+ 341.2

$B(E2) = 74(13)$

0^+

Experimental

$R_{exp} = 0.36$

4^+ 971

65

2^+ 355

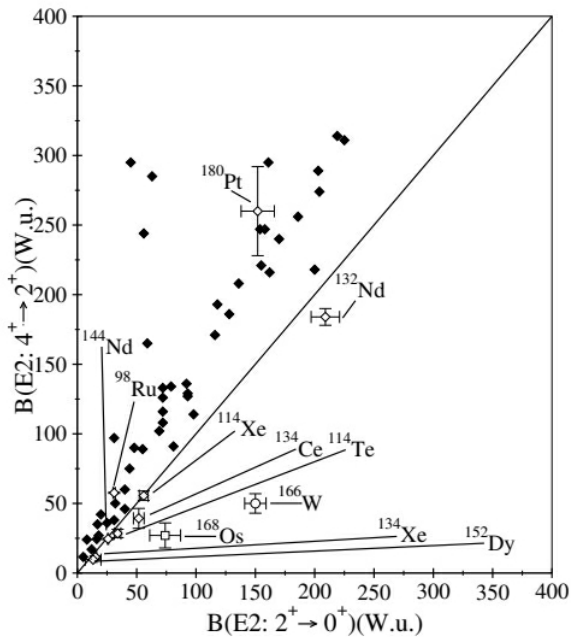
46

0^+ 0

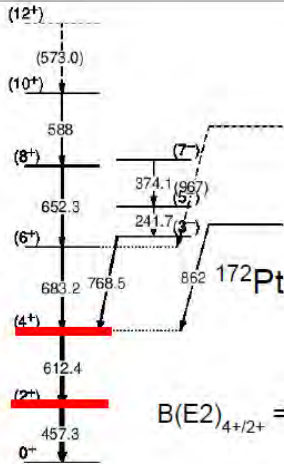
Theoretical

$R_{theo} = 1.41$

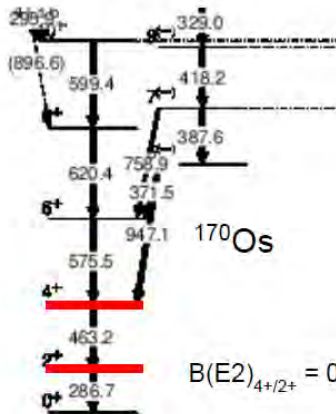
T. Grahn and B. Saygı et al. Phys. Rev. C,94, 044327



$$B(E2)_{4_1^+/2_1^+} \approx f(P.N)$$



$$B(E2)_{4_1^+/2_1^+} = 0.55$$

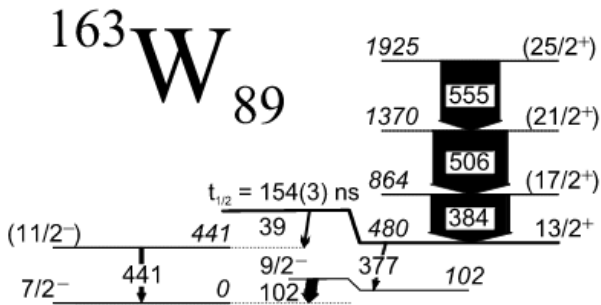


$$B(E2)_{4_1^+/2_1^+} = 0.38$$

Cederwall, B. et al. Phys. Rev. Lett., 121, 022502.

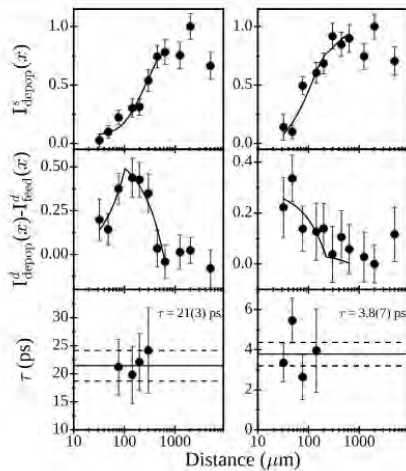
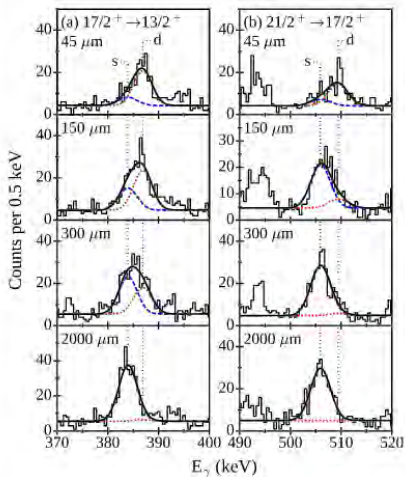
Goasduff, A. et al. Phys. Rev. C, 100, 034302.

$B(E2)_{4_1^+/2_1^+} \approx f(N.N) \text{ } ^{163}\text{W Case}$



- $^{106}\text{Cd}(^{60}\text{Ni}, 2\text{pn})^{163}\text{W}$
- DPUNS coupled to JUROGAM II
- 11 target-to-degrader distances

M.C. Lewis, D.T. Joss and B. Saygı et al. Phys. Lett. B 798 (2019) 134998

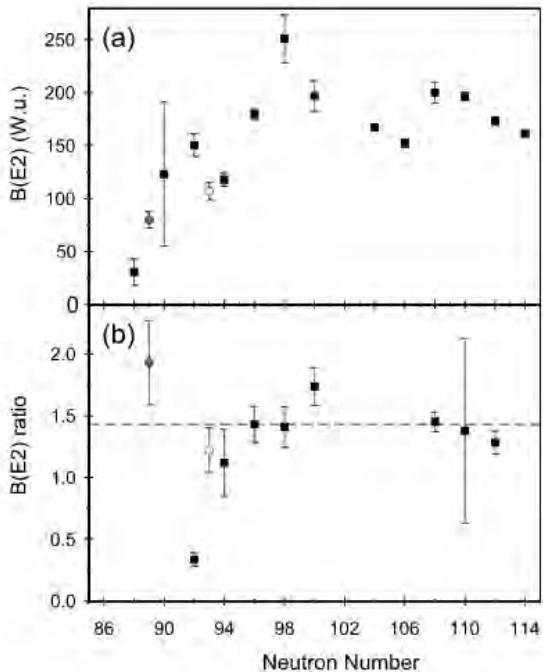


M.C. Lewis, D.T. Joss and B. Saygı et al. Phys. Lett. B 798 (2019) 134998

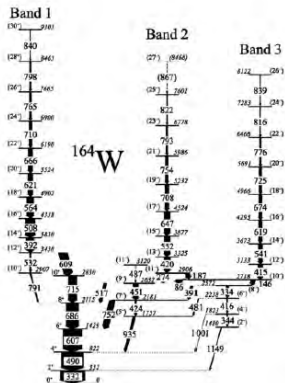
Table 1Measured lifetimes and reduced transition probabilities for excited states in ^{163}W .

E_γ (keV)	$I_i^\pi \rightarrow I_f^\pi$ (\hbar)	Detector angle	Recoil-correlated γ -ray coincidences	Isomer-tagged singles	Average values	
			τ (ps)	τ (ps)	τ (ps)	$B(E2)_{\downarrow}$ (W.u.)
384.1	$17/2^+ \rightarrow 13/2^+$	158°	21.3(30)	26.5(50)	22(2)	80(8)
		134°	21.4(30)			
		134°				
506.2	$21/2^+ \rightarrow 17/2^+$	158°	2.3(6)		3.0(4)	154(23)
		134°	3.8(7)			

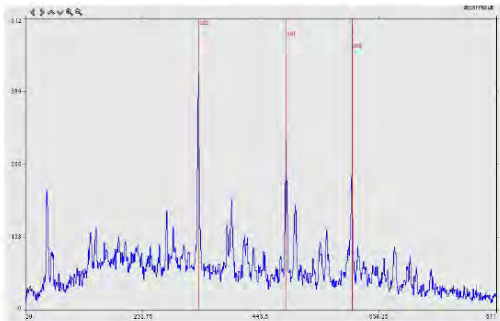
M.C. Lewis, D.T. Joss and B. Saygı et al. Phys. Lett. B 798 (2019) 134998



$B(E2)_{4_1^+/2_1^+} \approx f(N.N) \text{ } ^{164}\text{W Case}$



- In the experiment searching $^{163,164}\text{W}$ isotopes;
- $^{106}\text{Cd}(^{60}\text{Ni}, 2p)^{164}\text{W}^*$ at 270 MeV
- DPUNS coupled to JUROGAM II
- 11 Target-to-Degrader Distance used.



^{164}W has a similar $B(E2)_{4_1^+/2_1^+}=0.56(13)$
 B. Saygı et al. To be Published Data from JR139

TABLE I. Spin and parities of the yrast states in ^{170}Os together with their excitation energies, lifetimes, and reduced electromagnetic transition probabilities (experimental and theoretical). The reported theoretical values are the ones obtained in this work using the symmetry-conserving configuration mixing method.

J^π	E (keV)	τ (ps)	$I_i^\pi \rightarrow I_f^\pi$	$B(E2) \downarrow (e^2b^2)$	
				Expt.	Theor.
2_1^+	287	70_{-6}^{+6}	$2_1^+ \rightarrow 0_1^+$	$0.54_{-0.05}^{+0.05}$	0.53
4_1^+	750	18_{-4}^{+6}	$4_1^+ \rightarrow 2_1^+$	$0.21_{-0.04}^{+0.07}$	0.81

Goasduff, A. et al. Phys. Rev. C,100,034302.

- Symmetry conserving configuration mixing (SCCM) calculations were performed using the generator coordinate method framework with Hartree-Fock-Bogoliubov states found with variation after particle number projection (PN-VAP)
- The only benchmark situation in which $B(E2)_{4_1^+/2_1^+} < 1$ occurs where seniority is a good quantum number and from phenomenological point of view, a quantum phase transition from seniority-conserving structure to a collective regime as a function of neutron number around $N \approx 90-94$ has been proposed for these nuclei
- From theoretical point of view, the origin and the underlying structure giving rise to this anomalous behaviour remains unexplained up to date. These observations have not been reproduced so far by any type of state-of-the-art nuclear structure calculations, neither large-scale shell models nor beyond-mean-field models

Cederwall, B. et al. Phys. Rev. Lett.,121, 022502.

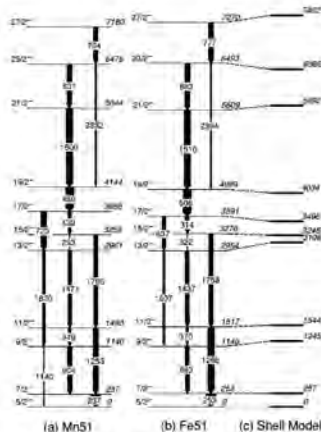
T. R. Rodríguez and J. L. Egido, Phys. Rev. C 84, 051307(R) (2011).

T. R. Rodríguez and J. L. Egido, Phys. Lett. B 705, 255 (2011).

$$B(E2)_{4_1^+/2_1^+} \approx f(N_p, N_n)$$

NpNn Scheme

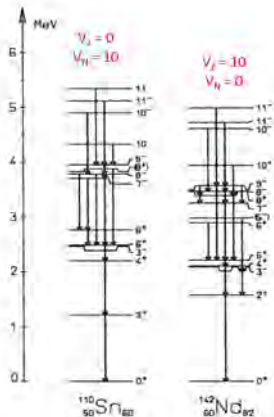
- NpNn scheme is introduced by Federman and Pittel and broadly used by Casten.
- Physics meaning of NpNn: a measure of integrated neutron-proton interaction.
- Symmetry of neutron-proton or related particle-hole arises from the isospin concept, which introduced by Heisenberg and states that neutron and proton and their related holes are different states of a nucleon.
- Experimental reflection of the isospin symmetry is quite well known.



M.A. Bentley, PRC, 62, 5 (1998)

NpNn Scheme

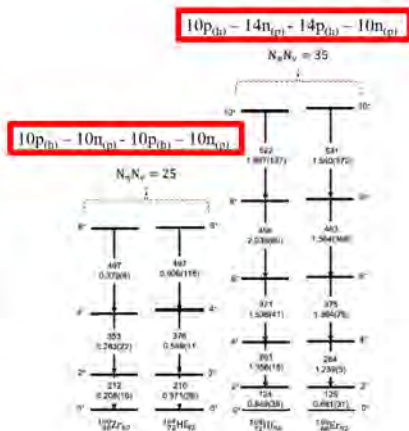
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J. Yun et. al, PRC, 62, 743, 1999

NpNn Scheme

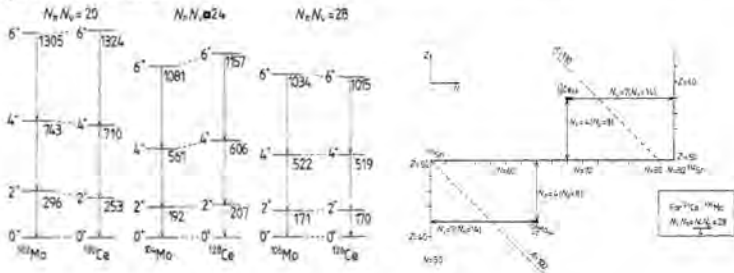
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B. Saygi, Nuclear Physics A, 980 (2018) 15-20

Pseudo-mirror nuclei

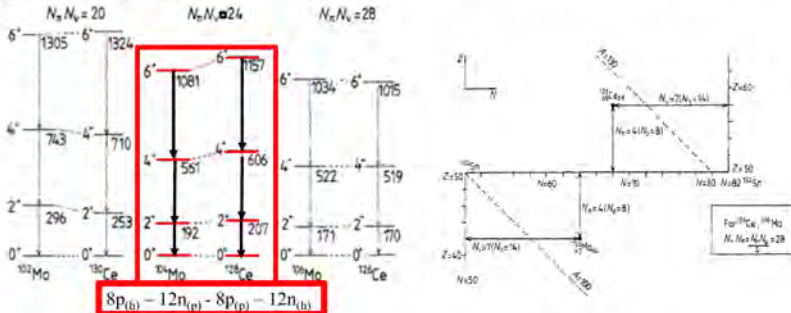
Pseudo-mirror nuclei (PMN) have been introduced by Moscrop et.al for the first time through the end of 80's.



R. Moscrop et.al, J. of Physics G: Nucl. and Phys., vol. 14, pp. L189, 1989.

Pseudo-mirror nuclei

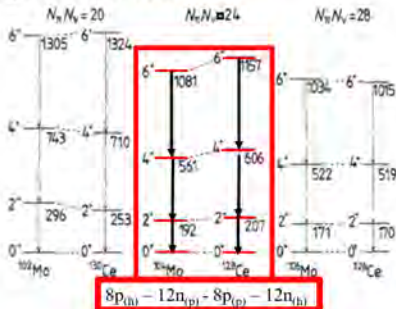
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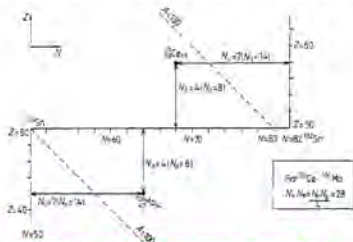
Pseudo-mirror nuclei

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Proton/Neutron - midshell

28 - 39 - Mo (42) - 50 50 - Ce (58) - 64 - 82
50 - Mo (62) - 64 - 82 50 - 64 - Ce (70) - 82



The NpNn is the product of valence neutrons (holes) and protons (holes) numbers.

R. Moscrop et.al, J. of Physics G: Nucl. and Phys., vol. 14, pp. L189, 1989.

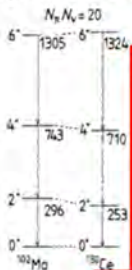
Pseudo-mirror nuclei

Proton/Neutron - midshell

Pseudo-mirror nuclei through the end of 80's

Pseudo-mirror nuclei (PMN) have been introduced by Moscrop et.al for the first time through the end of 80's over 12 nuclei

et.al for the first time



$N_p, N_n = 24$

$N_p, N_n = 28$

28 - 39 - Mo (42) - 50

50 - Mo (62) - 64 - 82

50 - Ce (58) - 64 - 82

50 - 64 - Ce (70) - 82

Table 1. New candidates for pseudo-mirror nuclei.

N_p, N_n	Nuclei	
15	¹³⁶ Nd	¹⁶⁰ Hf
16	¹³² Ce	¹⁶⁴ W
18	¹⁰⁶ Ru	¹²⁶ Ba
21	¹⁰⁸ Ru	¹²⁴ Ba
25	¹⁶⁴ Hf	
30	¹⁶⁶ Hf	¹⁶² Yb
35	¹⁰⁴ Zr	¹²⁸ Nd
		¹⁶⁸ Hf
		¹⁶⁰ Er

figure 1

figure 1

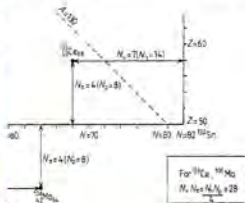
figure 1

figure 2

figure 3

figure 4

figure 5



B. Saygı, J. of Physics G: Nucl. and Part.

Phys. 45, 095104, 2018

$8p(h) - 1$

n is the product of valence neutrons (holes) and protons (holes) numbers

R. Moscrop et.al, J. of Physics G: Nucl. and Phys., vol. 14, pp. L189, 1989.

NpNn Scheme

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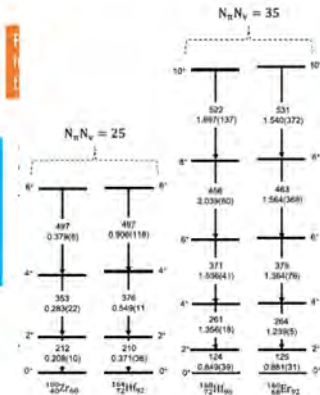
Systematics between $B(E2)$'s

$$\begin{aligned}
 B(E2; L^+ \rightarrow (L-2)^+)_{A \equiv 130} / B(E2; L^+ \rightarrow (L-2)^+)_{A \equiv 100} &\equiv 2_v \\
 B(E2; L^+ \rightarrow (L-2)^+)_{A \equiv 160} / B(E2; L^+ \rightarrow (L-2)^+)_{A \equiv 100} &\equiv 2_v \\
 B(E2; L^+ \rightarrow (L-2)^+)_{A \equiv 170} / B(E2; L^+ \rightarrow (L-2)^+)_{A \equiv 160} &\equiv 1_v \\
 B(E2; L^+ \rightarrow (L-2)^+)_{A \equiv 170, 160} / B(E2; L^+ \rightarrow (L-2)^+)_{A \equiv 130} &\equiv 1
 \end{aligned}$$

B. Saygi, J. of Physics G: Nucl. and Part. Phys. 45, 095104, 2018

nucleon.

- Experimental reflection of the isospin symmetry is quite well known.



B. Saygi, Nuclear Physics A, 980 (2018) 15-20

NpNn Scheme

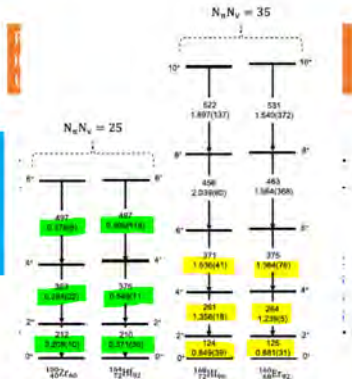
- NpNn scheme is introduced by Federman and Pittel and broadly used by Casten.

Physics meaning of NpNn: a measure of

- Systematics between B(E2)'s
- $B(E2; L^+ \rightarrow (L-2)^+)_{A=130} / B(E2; L^+ \rightarrow (L-2)^+)_{A=100} \equiv 2$,
- $B(E2; L^+ \rightarrow (L-2)^+)_{A=160} / B(E2; L^+ \rightarrow (L-2)^+)_{A=100} \equiv 2$,
- $B(E2; L^+ \rightarrow (L-2)^+)_{A=170} / B(E2; L^+ \rightarrow (L-2)^+)_{A=160} \equiv 1$,
- $B(E2; L^+ \rightarrow (L-2)^+)_{A=170/160} / B(E2; L^+ \rightarrow (L-2)^+)_{A=130} \equiv 1$
- B. Saygi, J. of Physics G: Nucl. and Part. Phys. 45, 095104, 2018

nucleon.

- Experimental reflection of the isospin symmetry is quite well known.



B. Saygi, Nuclear Physics A, 980 (2018) 15-20

Predictive power

Nuclide	2^+	4^+
^{102}Zr		≈ 0.500
^{106}Ru		≈ 0.250
^{124}Ba		≈ 0.610
^{128}Nd	≈ 0.800	
^{130}Nd		≈ 1.090
^{164}W	≈ 0.400	≈ 0.820

B. Saygi, J. of Phys. G: Nucl. And

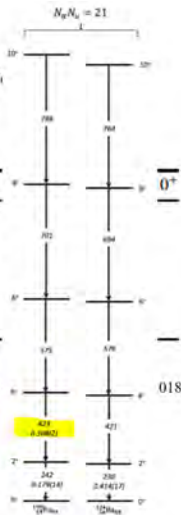


Table 1. Preliminary mean lifetimes and reduced electromagnetic transition probabilities in the yrast band of ^{124}Ba derived in this work. The values shown in the table are the average from the results for forward and backward rings.

E_{lev} [keV]	I^π	E_γ [keV]	τ [ps]	$B(E2)$ [e ² b ²]
651.7	4 ⁺	421.1	9.1 (8)	0.664 (58)
1228.4	6 ⁺	576.5	2.1 (2)	0.6 (1)
1923.3	8 ⁺	694.7	1.2 (4)	0.425 (148)

M. Trichkova, EPJ Web of Conferences 194, 03004 (2018)

Predictive power

Nuclide	2^+	4^+
^{102}Zr		≈ 0.500
^{106}Ru		≈ 0.250
^{124}Ba		≈ 0.610
^{128}Nd	≈ 0.800	
^{130}Nd		≈ 1.090
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- Systematics between $B(E2)$'s
- $B(E2; L^+ \rightarrow (L-2)^+)_{A=130} / B(E2; L^+ \rightarrow (L-2)^+)_{A=100} \equiv 2$

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Table 1. Preliminary mean lifetimes and reduced electromagnetic transition probabilities in the yrast band of ^{124}Ba derived in this work. The values shown in the table are the average from the results for forward and backward rings.

E_{dec} [keV]	I^π	E_γ [keV]	τ [ps]	$B(E2)$ [e ² b ²]
651.7	4^+	421.1	9.1 (8)	0.663 (58)
1228.4	6^+	576.5	2.1 (2)	0.6 (1)
1923.3	8^+	694.7	1.2 (4)	0.425 (148)

B. Saygı, J. of Phys. G: Nucl. And



M. Trichkova, EPJ Web of Conferences 194, 03004 (2018)

- Deformed mean field and self-consistent Hartree-Fock (SCHF) Hamiltonian

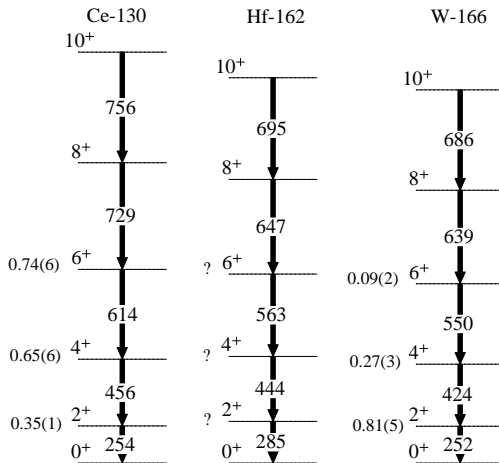
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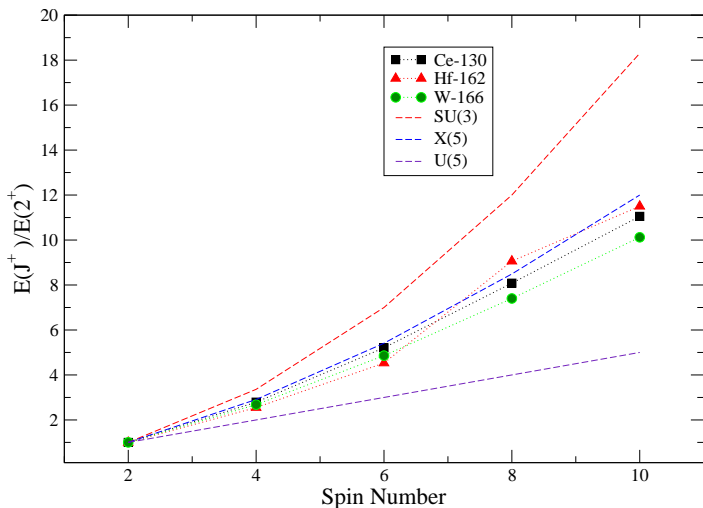
$$\hat{H} = \hat{H}_0 + \frac{1}{2}\kappa_{nn}\hat{Q}_n\hat{Q}_n + \frac{1}{2}\kappa_{pp}\hat{Q}_p\hat{Q}_p + \kappa_{np}\hat{Q}_n\hat{Q}_p, \quad (1)$$

- \hat{H}_0 is the spherical single-particle Hamiltonian
- κ 's are the coupling constants.
- The relation of the κ 's is that $\kappa_{np} \approx 5\kappa_{pp} \approx 5\kappa_{nn}$
- Indicating that n-p ($\hat{Q}_n\hat{Q}_p$) interaction dominates while building the nuclear deformation.

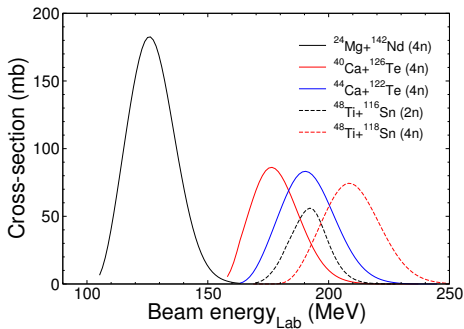
J. Dobaczewskiet al., Phys. Rev. Lett. 60 (1988) 2254.

$N_p N_n = 80$

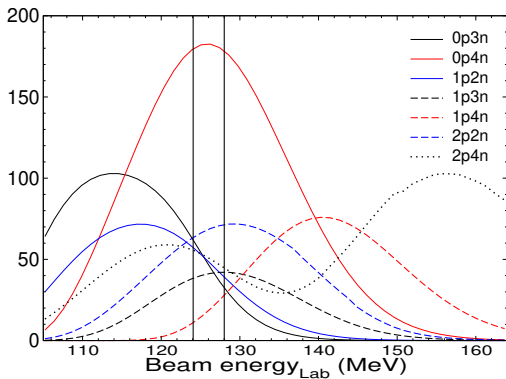




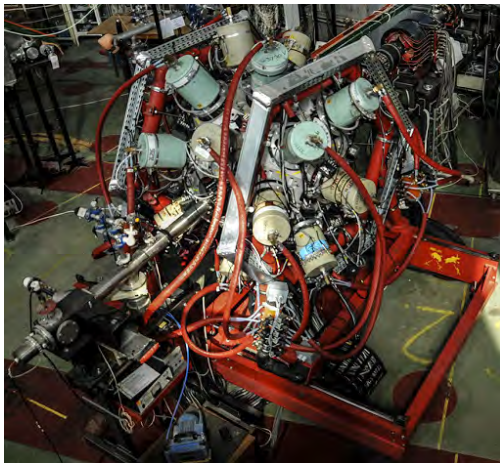
Systematics of excitation energies values in neutron-deficient even-even ^{130}Ce , ^{162}Hf and ^{166}W nuclides. Calculated ratio using the IBM in the SU(3), X(5) and U(5) limits are also reported. Excitation energy of the yrast state normalized to the $E(2_1^+)$



Comparison of reaction of interest with possible reactions to populate $^{162}\text{Hf}^*$ reaction.



Comparison of reaction channels of interest with possible reaction channels in $^{142}\text{Nd}(^{24}\text{Mg},4n)^{162}\text{Hf}^*$ reaction.





UNIVERSITY
OF WARSAW

Heavy Ion Laboratory



Warsaw, 25.05.2020

Prof. Krzysztof Rusek
Director
Heavy Ion Laboratory
University of Warsaw
Warsaw, Poland

Dr. Bahadır SAYGI
Ege University
Science Faculty
Physics Department
İzmir, Turkey

Dear Spokesperson Dr. Saygi,

I would like to inform that your proposal entitled "Lifetime measurement of excited states in ^{180}Hf " has been accepted by the Heavy Ion Laboratory Program Advisory Committee meeting held on the 17th of December 2019. The PAC recommends that your experiment should be performed with the total number of requested 21 shifts. The code HIL092 has been assigned for your experiment. You will be notified about the beam-time schedule, when it is available.

For any additional information please do not hesitate to contact the PAC Secretary.

Best regards,

- The NEutron Detector Array, NEDA, will form the next generation neutron detection system that has been designed to be operated in conjunction with γ -ray arrays, such as the tracking-array AGATA, to aid nuclear spectroscopy studies.
- NEDA has been designed to be a versatile device, with high-detection efficiency, excellent neutron- discrimination, and high rate capabilities.
- It will be employed in physics campaigns in order to maximise the scientific output, making use of the different stable and radioactive ion beams available in Europe.
- The first implementation of the neutron detector array NEDA with AGATA 1π was realised at GANIL. This manuscript reviews the various aspects of NEDA.

J.J. Valiente-Dobón, G. Jaworski, A. Goasduff, ..., B. Saygı et al. Nuclear Inst. and Methods in Physics Research, A 927 (2019) 81–8



- Dr. G. Jaworski got a funding from The Polish Academy of Sciences in order to host NEDA at Heavy Ion Laboratory in Warsaw, Poland.
- As an international collaborator, we have contributed with 3 experimental idea in order to investigate $B(E2)_{4_1^+/2_1^+}$ and gather more experimental data for future theoretical calculations.
- EAGLE array will be employed in junction with NEDA and plunger
- Data is planned to be collected using RDDS technique
- Data is planned to be analysed with DDCM in coincidence mode.

Core Collaboration



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