



SELCUK UNIVERSITY
FACULTY OF SCIENCE



XIV. International Conference On Nuclear Structure Properties

We are pleased to announce the XIV. International Conference on Nuclear Structure Properties, NSP2021 to be held as online meeting on 2-4 June 2021 in Selcuk University, Konya, TURKEY.

2-4 June 2021

Conference web page: <http://nsp2021.selcuk.edu.tr>

XIV INTERNATIONAL CONFERENCE ON NUCLEAR STRUCTURE PROPERTIES
2 – 4 JUNE 2021
SELCUK UNIVERSITY, KONYA ,TURKEY

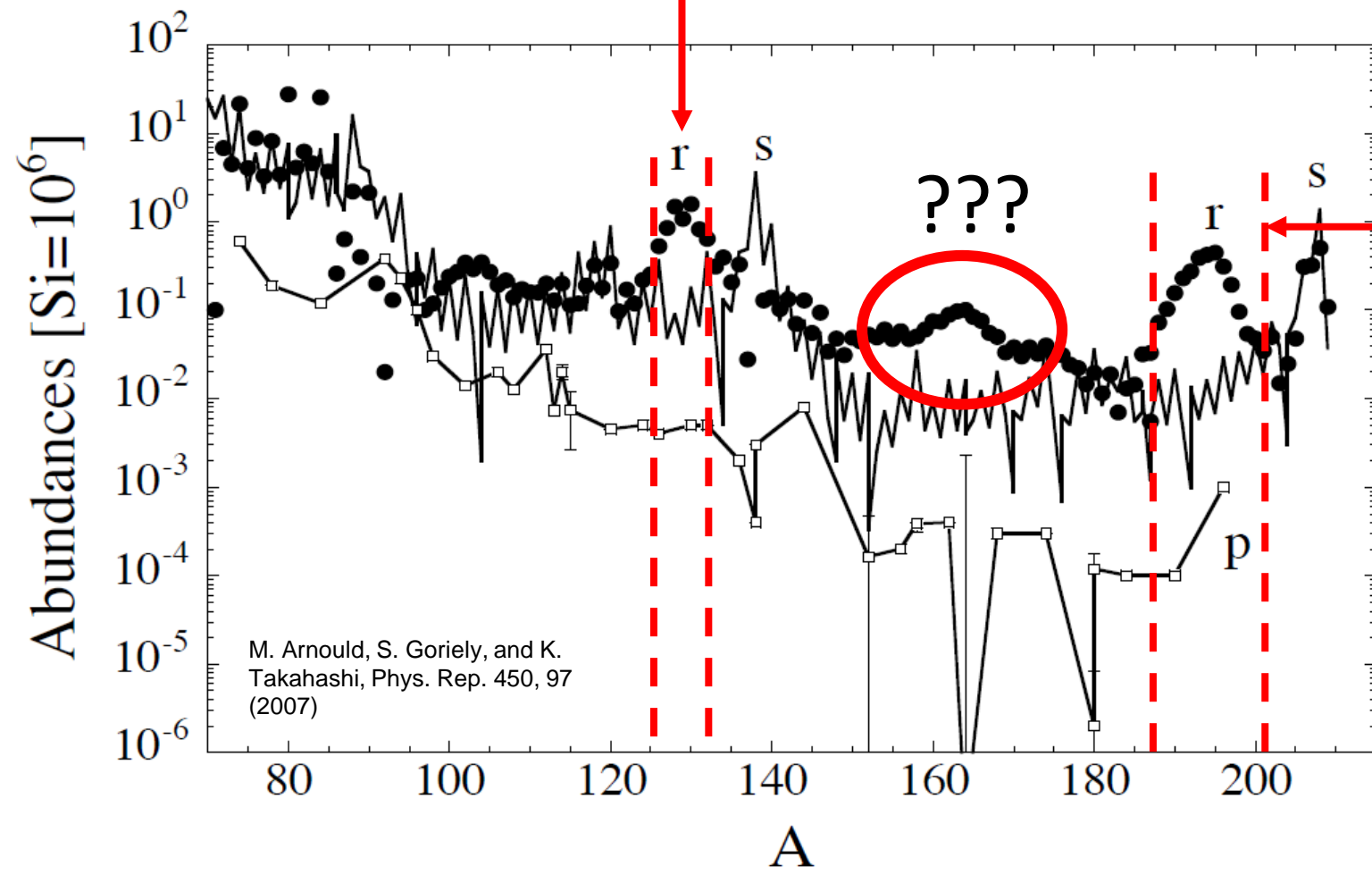
Role of nuclear tensor force within Skyrme mean-field approach on deformed magic numbers in rare earth region

DR. KOH MENG HOCK

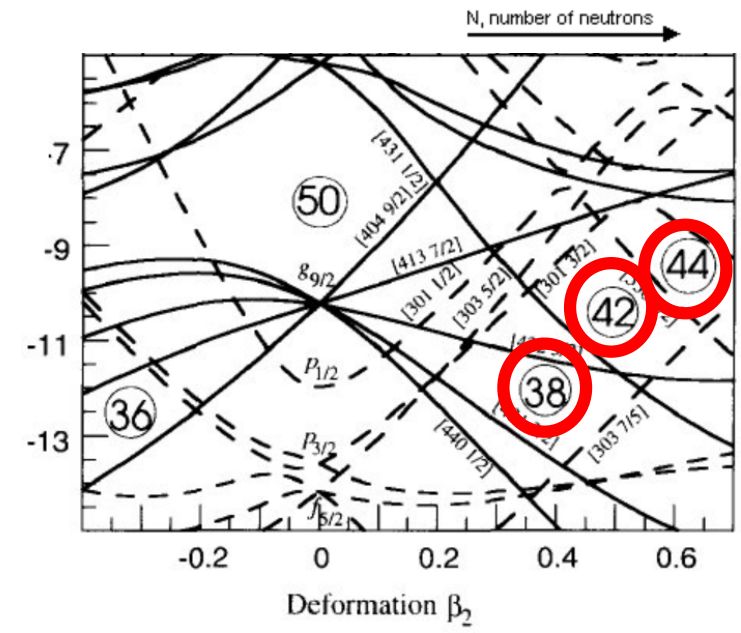
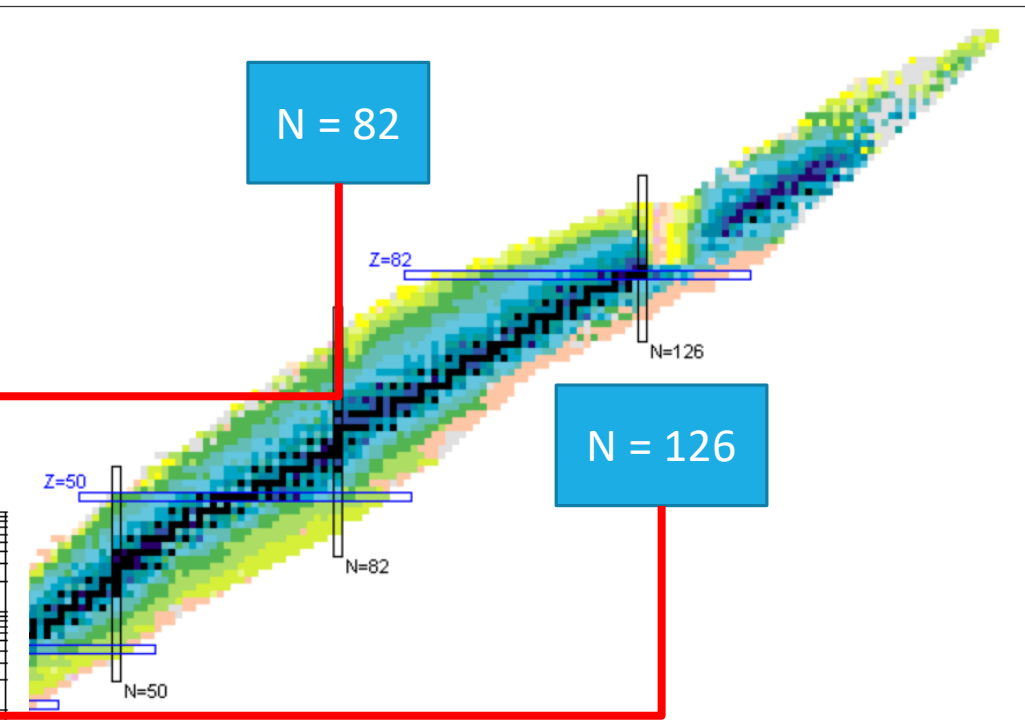
DEPARTMENT OF PHYSICS
FACULTY OF SCIENCE, UNIVERSITI TEKNOLOGI MALAYSIA

Solar abundance around mass number 165

Abundance of elements due to neutron shell closures



Z , number of protons



Studies on deformed magic numbers

An abstract background graphic on the right side of the slide. It consists of a dense network of thin, light gray lines connecting numerous circular nodes of varying sizes. The nodes are also light gray, creating a complex, web-like structure that fills the right half of the slide.

BRIEF ACCOUNT OF EXPERIMENTAL WORK

A solid teal horizontal bar at the bottom of the slide, spanning the entire width.

Skyrme force with and without tensor

Skyrme Hamiltonian density

Many-body Hamiltonian $\longrightarrow \hat{H} = \hat{K} + \hat{V}$

Effective nucleon-nucleon interaction

Approximated by the
Skyrme force

$$V(\mathbf{r}_1, \mathbf{r}_2) = V_c(\mathbf{r}_1, \mathbf{r}_2) + V_{DD}(\mathbf{r}_1, \mathbf{r}_2) + V_{s.o}(\mathbf{r}_1, \mathbf{r}_2)$$

Central
potential

Density
dependent
potential

Spin-orbit
potential

+ V_{tensor}

$$\mathcal{H} = B_1 \rho^2 + B_3 (\rho \tau - \mathbf{j}^2) + B_5 \rho \Delta \rho + B_7 \rho^{2+\alpha} \\ + B_9 (\rho \nabla \cdot \mathbf{J} + \mathbf{j} \cdot \nabla \times \mathbf{s}) + B_{10} s^2 + B_{12} \rho^\alpha s^2$$

$$+ B_{14} \left(\sum_{\mu, \nu=x}^z \mathbf{J}_{\mu\nu} \mathbf{J}_{\mu\nu} - \mathbf{s} \cdot \mathbf{T} \right) \\ + B_{16} \left[\left(\sum_{\mu=x}^z \mathbf{J}_{\mu\mu} \right)^2 + \left(\sum_{\mu, \nu=x}^z \mathbf{J}_{\mu\nu} \mathbf{J}_{\nu\mu} - 2 \mathbf{s} \cdot \mathbf{F} \right) \right] \\ + B_{18} \mathbf{s} \cdot \Delta \mathbf{s} + B_{20} (\nabla \cdot \mathbf{s})^2$$

$$\mathcal{H}_q = B_2 \rho_q^2 + B_4 (\rho_q \tau_q - \mathbf{j}_q^2) + B_6 \rho_q \Delta \rho_q + B_8 \rho_0^\alpha \rho_q^2 \\ + B_{9_q} (\rho_q \nabla \cdot \mathbf{J}_q + \mathbf{j}_q \cdot \nabla \times \mathbf{s}_q) + B_{11} s_q^2 + B_{13} \rho^\alpha s_q^2$$

$$+ B_{15} \left(\sum_{\mu, \nu=x}^z \mathbf{J}_{q, \mu\nu} \mathbf{J}_{q, \mu\nu} - \mathbf{s}_q \cdot \mathbf{T}_q \right) \\ + B_{17} \left[\left(\sum_{\mu=x}^z \mathbf{J}_{q, \mu\mu} \right)^2 + \left(\sum_{\mu, \nu=x}^z \mathbf{J}_{q, \mu\nu} \mathbf{J}_{q, \nu\mu} - 2 \mathbf{s}_q \cdot \mathbf{F}_q \right) \right] \\ + B_{19} \mathbf{s}_q \cdot \Delta \mathbf{s}_q + B_{21} (\nabla \cdot \mathbf{s}_q)^2$$

Skyrme Hamiltonian density

$$\begin{aligned}\mathcal{H} = & B_1 \rho^2 + B_3 (\rho\tau - \mathbf{j}^2) + B_5 \rho\Delta\rho + B_7 \rho^{2+\alpha} \\ & + B_9 (\rho\nabla \cdot \mathbf{J} + \mathbf{j} \cdot \nabla \times \mathbf{s}) + B_{10} \mathbf{s}^2 + B_{12} \rho^\alpha \mathbf{s}^2 \\ & + B_{14} \left(\sum_{\mu,\nu=x}^z \mathbf{J}_{\mu\nu} \mathbf{J}_{\mu\nu} - \mathbf{s} \cdot \mathbf{T} \right) \\ & + B_{16} \left[\left(\sum_{\mu=x}^z \mathbf{J}_{\mu\mu} \right)^2 + \left(\sum_{\mu,\nu=x}^z \mathbf{J}_{\mu\nu} \mathbf{J}_{\nu\mu} - 2 \mathbf{s} \cdot \mathbf{F} \right) \right] \\ & + B_{18} \mathbf{s} \cdot \Delta \mathbf{s} + B_{20} (\nabla \cdot \mathbf{s})^2\end{aligned}$$

$$B_{14} = \underbrace{-\frac{t_1 x_1 + t_2 x_2}{8}}_{\text{Central components}} + \underbrace{\frac{1}{4}(t_e + t_o)}_{\text{Tensor components}}$$

$$B_{16} = -\frac{3}{8}(t_e + t_o)$$

Tensor only

Skyrme forces with tensor

Perturbative fit

Original Skyrme parameters
+
Fit of two tensor parameters



Available online at www.sciencedirect.com



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www.elsevier.com/locate/physletb

Spin–orbit splitting and the tensor component of the Skyrme interaction

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THE TENSOR PART OF SKYRME'S INTERACTION

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PHYSICAL REVIEW C **97**, 064304 (2018)

Skyrme density functional description of the double magic ⁷⁸Ni nucleus

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We calculate the single-particle spectrum of the double magic nucleus ⁷⁸Ni in a Hartree-Fock approach using the Skyrme density-dependent effective interaction containing central, spin-orbit, and tensor parts. We show that the tensor part has an important effect on the spin-orbit splitting of the proton 1*f* orbit that may explain the survival of magicity so far from the stability valley. We confirm the inversion of the 1*f*5/2 and 2*p*3/2 levels at the neutron number 48 in the Ni isotopic chain expected from previous Monte Carlo shell-model calculations and supported by experimental observation.

Skyrme forces with tensor

Full refit

Refit of all original 10 parameters
+
2 tensor parameters

PHYSICAL REVIEW C **76**, 014312 (2007)

Tensor part of the Skyrme energy density functional: Spherical nuclei

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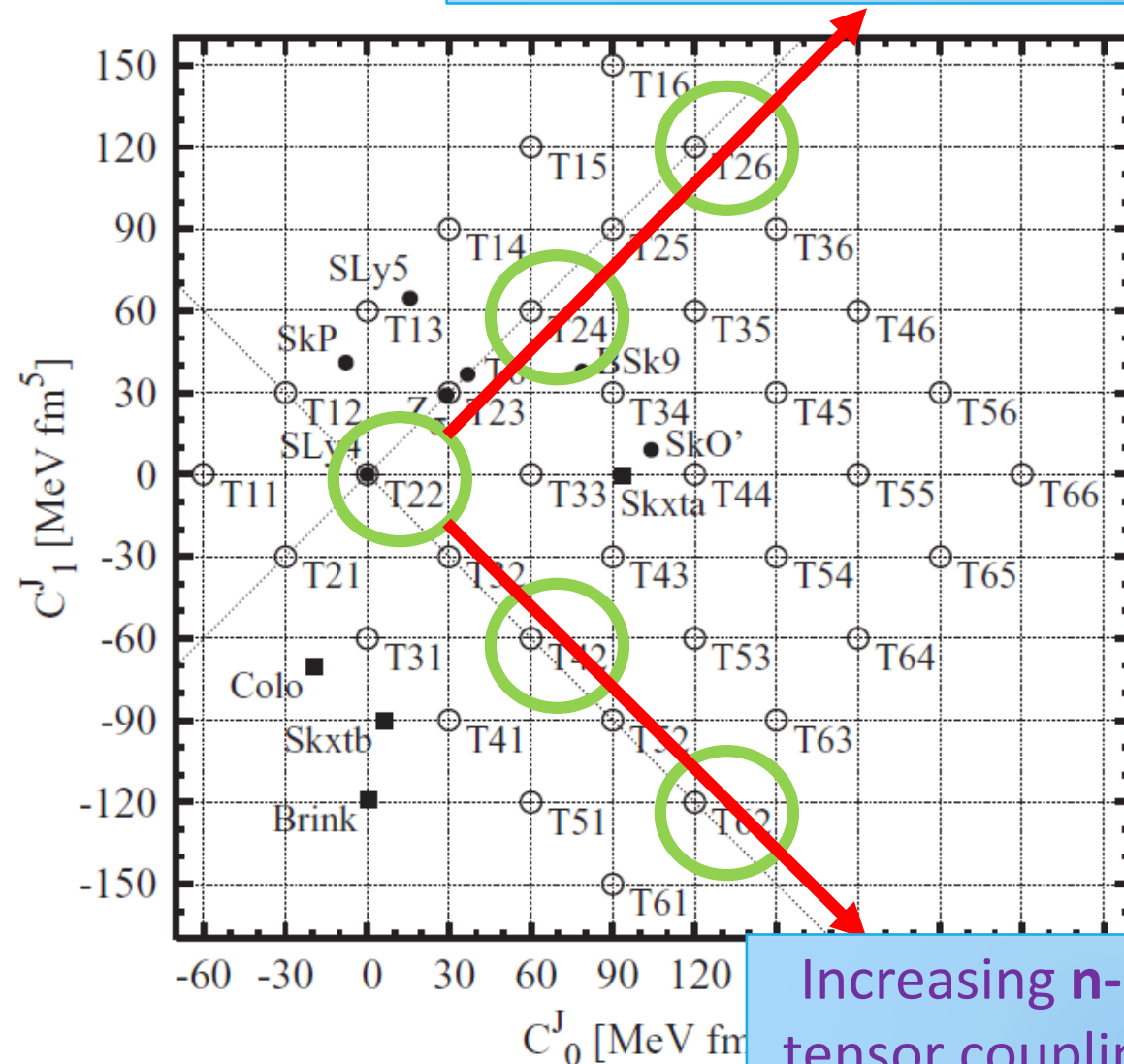
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Increasing like-particle
tensor coupling



Increasing n-p
tensor coupling

Two-neutron separation energy differential

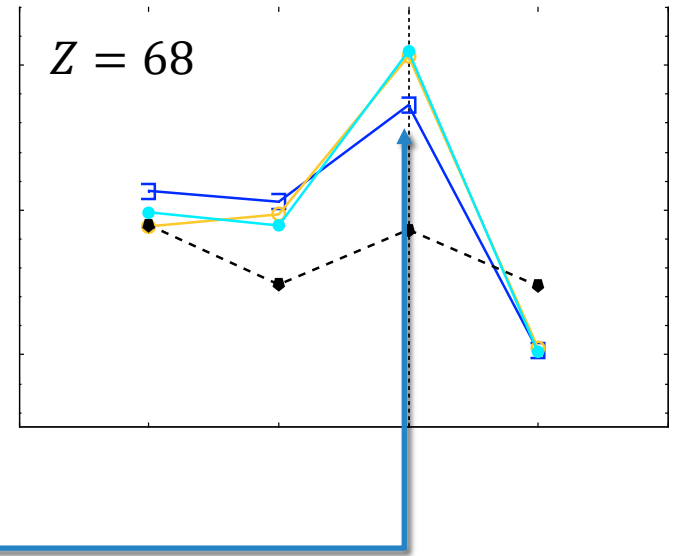
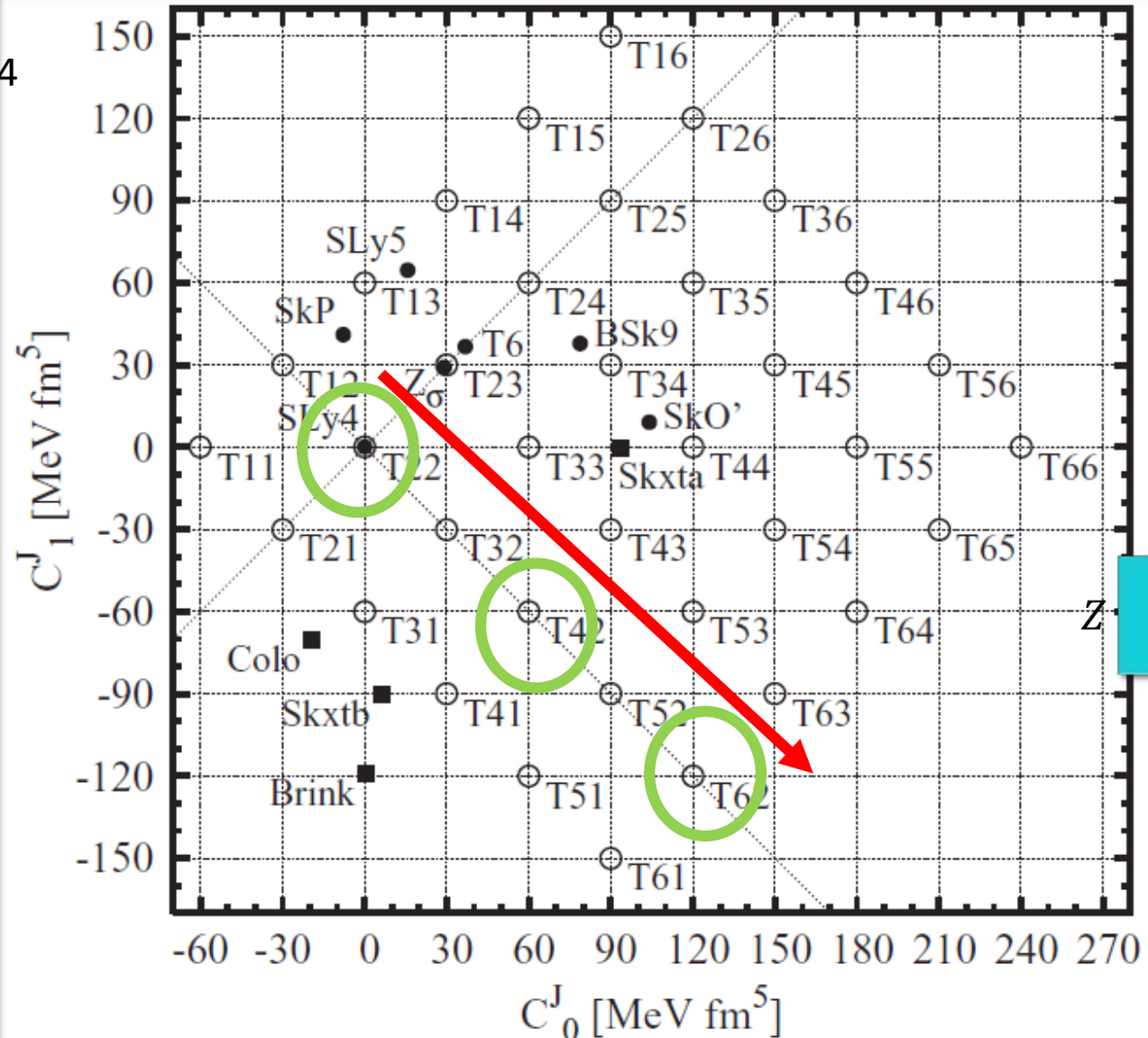
RESULTS

Experimental two-neutron separation energy differential

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-
-

-
-
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Two-neutron separation energy differential - Increasing np tensor coupling



What we learnt?

- T22 reproduce some experimental peaks
- Strong np tensor reinforce the peaks obtained by T22 at $N = 104$ in heavier RE

Two-neutron separation energy differential - Increasing nn and pp tensor coupling

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Extracting the tensor contribution

RESULTS

Contribution of tensor and non-tensor EDF terms to S2n differential T26 vs T22 vs T62 (Experimental peak at N = 104)

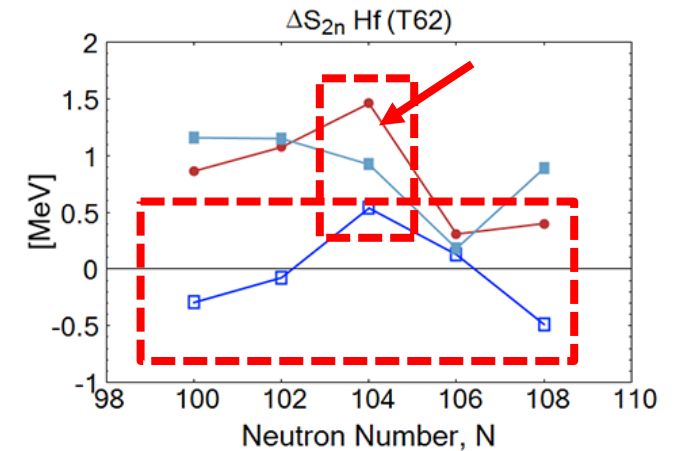
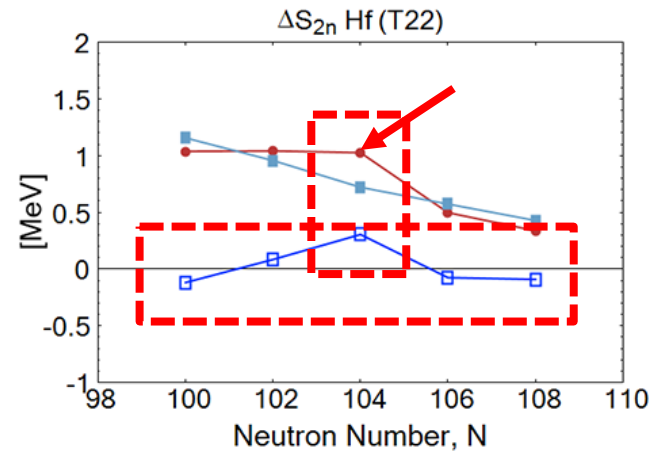
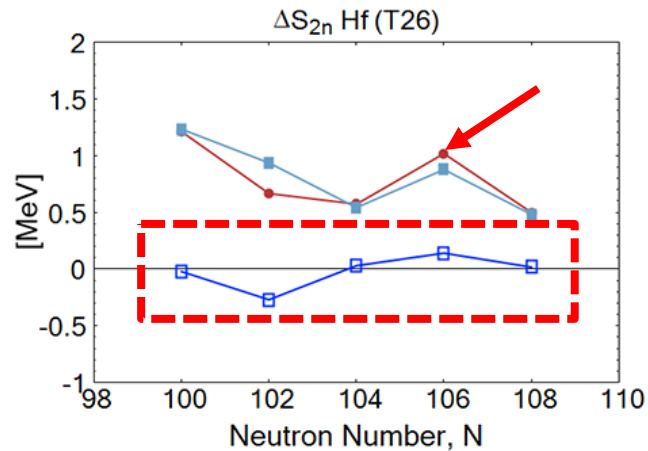
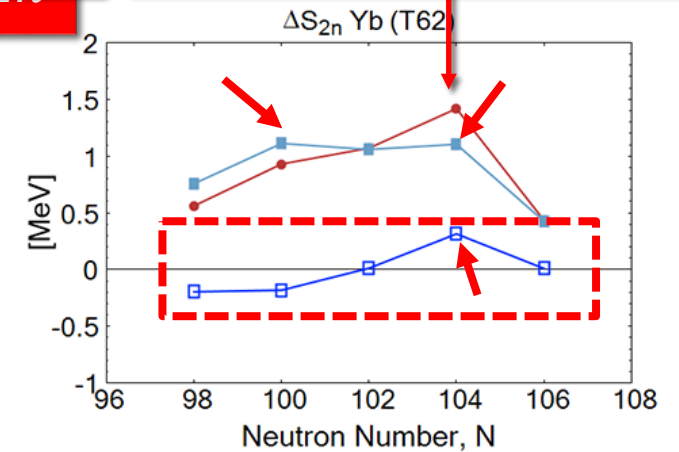
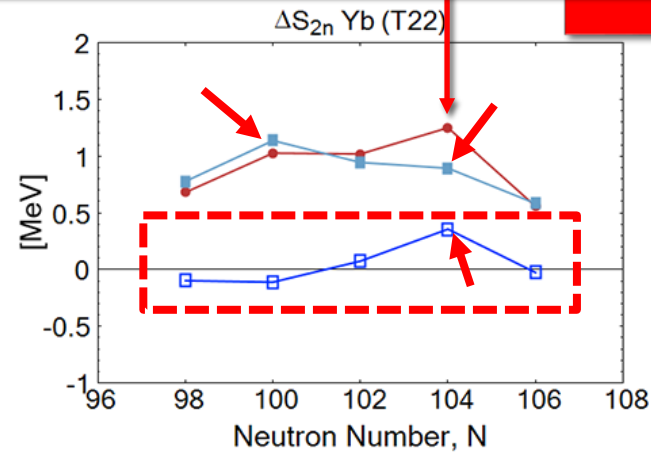
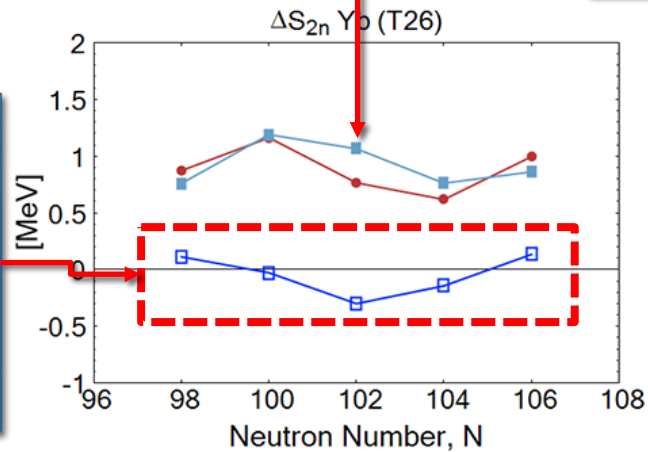
Central
contr.

Reflects the need for nuclear tensor.
*Note: Combinations of T22 tensor terms in the
EDF cancels one another.*

Neutron-proton tensor coupling
enhance the peak at N = 104.

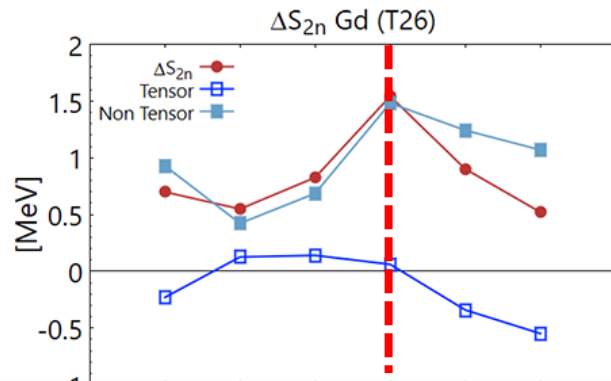
Tensor contr.

$$E_{B_{14}}^T + E_{B_{15}}^T \\ + E_{B_{16}} \\ + E_{B_{17}}$$

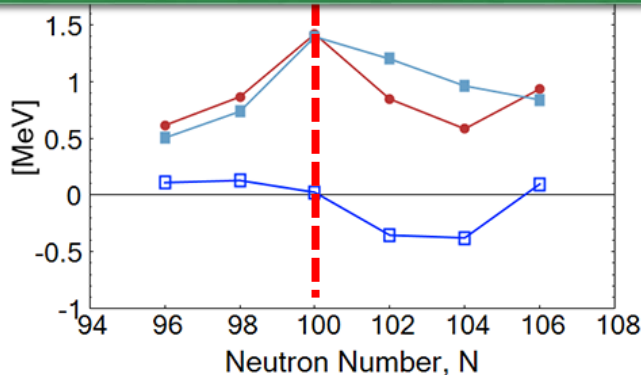


Contribution of tensor and non-tensor EDF terms to S2n differential T26 vs T22 vs T62 (Lighter RE at N = 98 and N = 102)

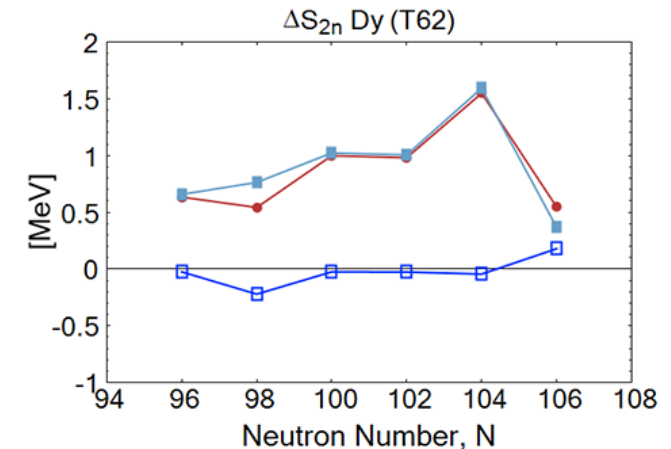
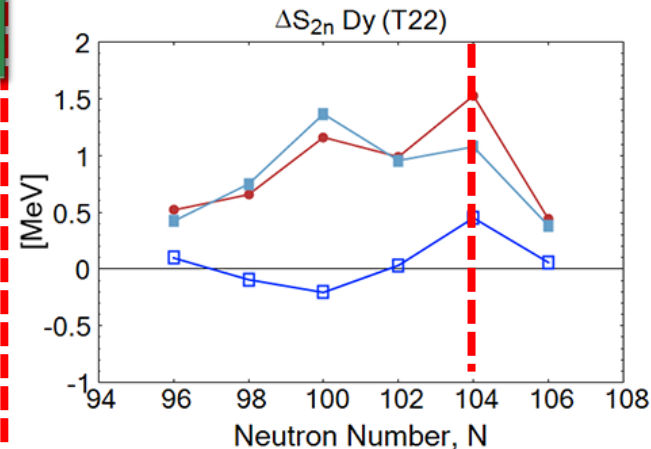
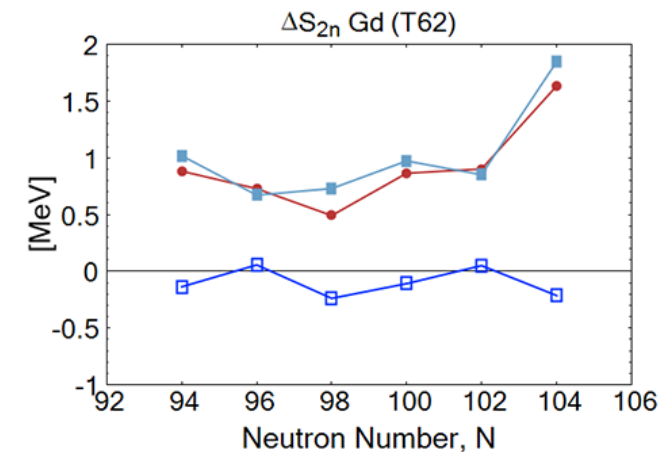
Peak at N = 104 is removed. Only a peak at N = 100.



Strong neutron-neutron and proton-proton tensor coupling might be the key to explain neutron magicity in lighter RE.



No peak appearing at N = 98 and N = 102 with strong n-p tensor coupling.



Summary

ROLE OF NUCLEAR TENSOR ON DEFORMED NUMBERS IN RARE
EARTH NUCLEI

Key message to take home...

1. Neutron magicity in heavy rare earth nuclei ($Z > 66$) – Strong neutron-proton tensor coupling is needed
2. Light rare earth nuclei ($Z \leq 66$)
 - a) Magicity at $N = 98$ and $N = 102$ is not reproduced, but ...
 - b) Increasing like-particle (nn and pp) tensor coupling might be the key ingredient
3. More experimental data are needed for example in
 - a. lighter ($Z \leq 62$) and heavier ($Z \geq 72$)
 - b. the whole RE region in general – to verify sometimes conflicting data (BE, half-life, excitation energy levels)

Questions
or
comments?

